

Circles Vocab and Arcs

IC1

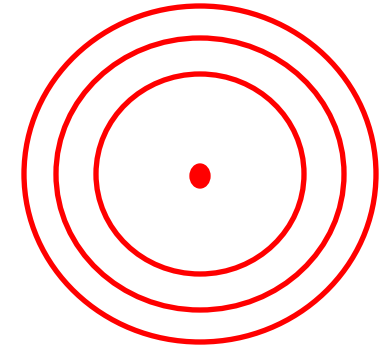
What is a circle?

A set of all points equidistant from a certain location (center of circle)

2. Circle A and circle B are concentric.

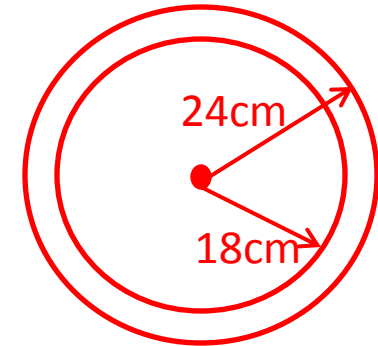
a) What does that mean?

Circles that share the same center



b) If the radius of circle A is 24 cm and the radius of circle B is 18 cm. What scale factor would map circle A onto circle B?

Big \rightarrow small (reduction requires a scale factor less than 1)



$$\frac{18}{24} = \frac{3}{4}$$

Circle Terminology:

Interior Point – Any point inside the circle	Exterior Point – Any point outside the circle
Major Arc – An arc MORE than $\frac{1}{2}$ the circle. *Named with 3 letters.	Minor Arc – An arc LESS than $\frac{1}{2}$ the circle. *Named with 2 letters.
Semi-Circle – An arc that is $\frac{1}{2}$ the circle.	Chord – A segment with both endpoints on the circle
Tangent Line – Line that passes through a circle once (touches)	Secant Line – Line that passes through a circle twice.
Central Angle – An angle at center formed by radii	

6. Match the following for Circle A.

a. 9 Major Arc

b. 7 Diameter

c. 7, 1 Chord

d. 5 Minor Arc

e. 10 Tangent line

f. 2, 4 Interior Point

g. 3 Secant line

h. 6 Exterior Point

i. 4 Center

j. 8 Semi-Circle

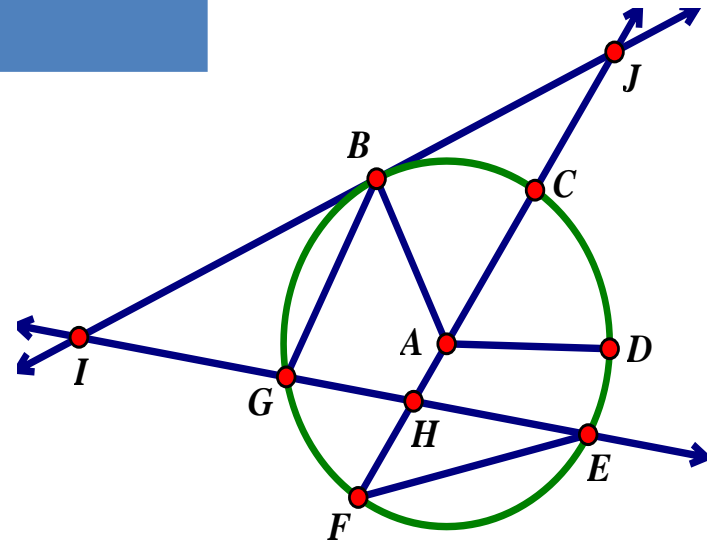
1. \overline{EG} 6. Point I

2. Point H 7. \overline{FC}

3. \overrightarrow{GE} 8. \widehat{CBF}

4. Point A 9. \widehat{CEG}

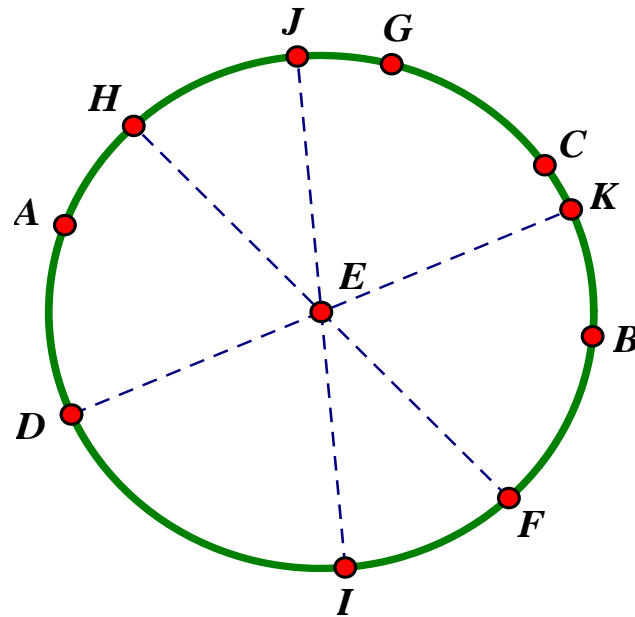
5. \widehat{FD} 10. \overrightarrow{IJ}



3. Determine whether the arc described is major, minor, or a semicircle.

a) F to G clockwise major b) A to F clockwise major

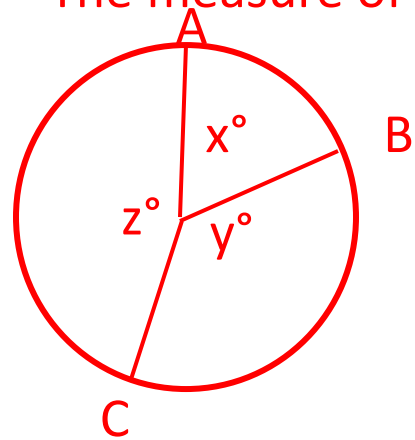
c) J to C clockwise minor d) K to D clockwise semicircle



Arc Measure:

A number of degrees which describes a portion of a circle's circumference.

The measure of an arc = the central angle measure that intersects the arc



$$m\widehat{AB} = x^\circ$$

$$m\widehat{BC} = y^\circ$$

$$m\widehat{AC} = z^\circ$$

$$m\widehat{ACB} = (z + y)^\circ$$

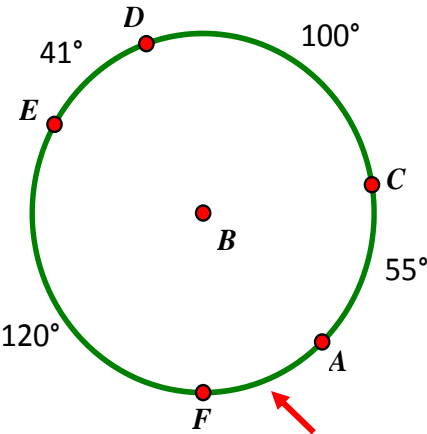
Helpful Hints:

- All non-overlapping arcs add to 360°
- Diameters divide circles in half → semi circles have 180° measure.
- Sometimes subtracting what's not included from 360° is a good strategy.

1. Determine the arc measure.

a)

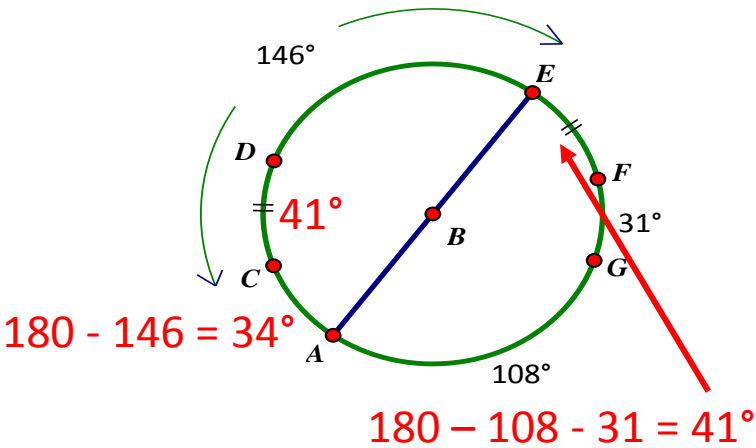
$m\widehat{DF} = 41^\circ + 120^\circ = 161^\circ$
 $m\widehat{ECA} = 41^\circ + 100^\circ + 55^\circ = 196^\circ$
 $m\widehat{AF} = 44^\circ$
 $m\widehat{CFD} = 55^\circ + 44^\circ + 120^\circ + 41^\circ = 260^\circ$
 $360^\circ - 100^\circ = 260^\circ$



$360 - 120 - 41 - 100 - 55 = 44^\circ$

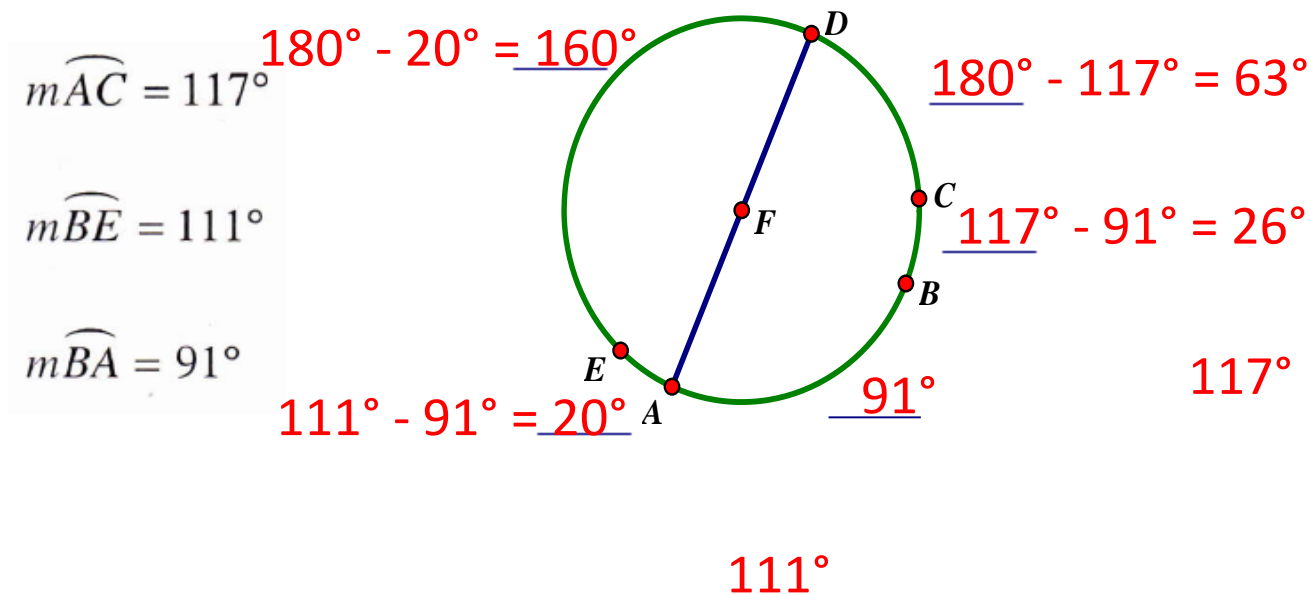
b)

$m\widehat{AC} = 34^\circ$
 $m\widehat{DAG} = 41^\circ + 34^\circ + 108^\circ = 183^\circ$
 $m\widehat{AD} = 41^\circ + 34^\circ = 75^\circ$
 $m\widehat{DAF} = 183^\circ + 31^\circ = 214^\circ$



2. Determine the measure of the missing arcs on the circle.

Given: Circle F



3. Determine the missing information.

a) Given concentric circles with $m\widehat{GF} = 76^\circ$, $m\angle HIE = 147^\circ$ and \overline{CA} & \overline{FH} are diameters

$m\widehat{CB} = \underline{104^\circ}$

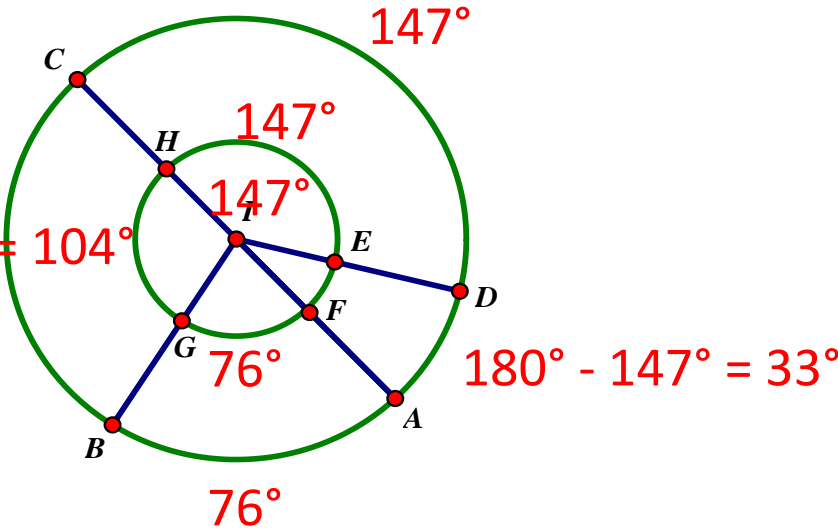
$m\widehat{HE} = \underline{147^\circ}$

$m\widehat{BDC} = 180^\circ + 76^\circ = 256^\circ$
 $360^\circ - 104^\circ = 256^\circ$

$m\angle CIB = \underline{104^\circ}$

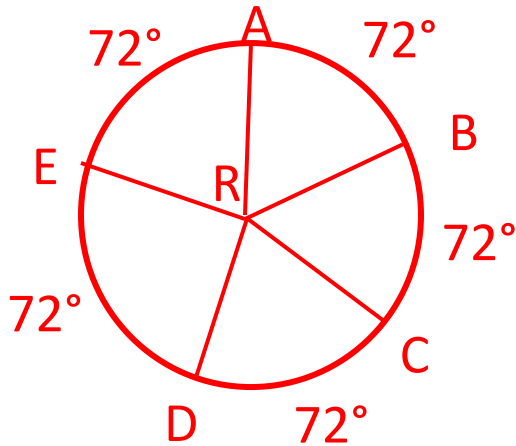


Central angle measures = arc measures



4. Points A, B, C, D, and E are placed on circle R in this order such that there are five congruent arcs.

What is the $m\widehat{BCE}$



$$\frac{360}{5} = 72^\circ$$

$$360^\circ - 144^\circ = 216^\circ$$

or

$$(72^\circ)(3) = 216^\circ$$