

Determine the imaginary roots of each equation by either using the quadratic formula or completing the square. Write all complex roots in standard form.

1. $y = x^2 + 5$

$$x = \frac{-0 \pm \sqrt{0^2 - 4(1)(5)}}{2(1)}$$

$$x = \frac{\pm \sqrt{0-20}}{2}$$

$$x = \frac{\pm \sqrt{-20}}{2}; \quad x = \frac{\pm 2i\sqrt{5}}{2}$$

$$x = \pm i\sqrt{5}$$

2. $y = 2x^2 + 5x + 4$

$$x = \frac{-5 \pm \sqrt{5^2 - 4(2)(4)}}{2(2)}$$

$$= \frac{-5 \pm \sqrt{25-32}}{4}$$

$$x = \frac{-5 \pm \sqrt{-7}}{4}$$

$$x = \frac{-5 \pm i\sqrt{7}}{4}$$

3. $y = x^2 - 2x + 3$

$$x = \frac{-(-2) \pm \sqrt{(-2)^2 - 4(1)(3)}}{2(1)}$$

$$= \frac{2 \pm \sqrt{4-12}}{2}$$

$$x = \frac{2 \pm \sqrt{-8}}{2}$$

$$x = \frac{2 \pm 2i\sqrt{2}}{2}$$

$$x = 1 \pm i\sqrt{2}$$

Perform the indicated operation and write the final expression in the form of $a+bi$.

4. $(3-5i) + (2+2i) = 5-3i$

5. $(1+2i) - (3-4i) = -2+6i$

6. $(5+i)(3-2i) = 15-7i-2i^2 = 17-7i$

$$7. (2-3i)^2 = (2-3i)(2-3i) = 4 - 12i + 9i^2 = 4 - 12i - 9 \\ = -5 - 12i$$

$$8. \frac{i}{1-i} \frac{(1+i)}{(1+i)} = \frac{i + i^2}{1 - i^2} = \frac{i - 1}{2} \text{ or } \frac{i}{2} - \frac{1}{2}$$

$$9. \frac{3-2i}{2+i} \frac{(2-i)}{(2-i)} = \frac{6 - 7i + 2i^2}{4 - i^2} = \frac{4 - 7i}{5} \text{ or } \frac{4}{5} - \frac{7}{5}i$$