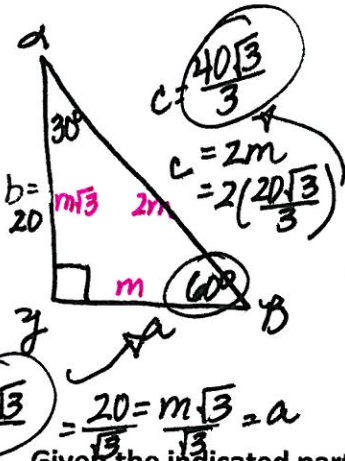
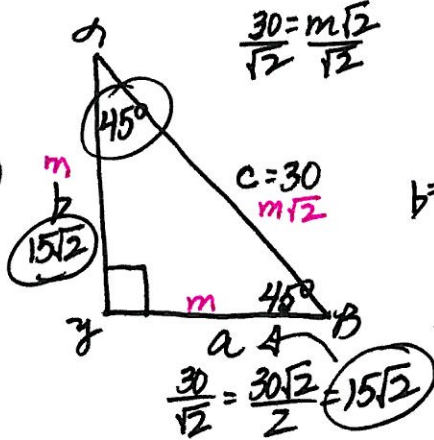


Given the indicated parts of triangle ABC with $\gamma = 90^\circ$, find the exact values of the remaining parts.

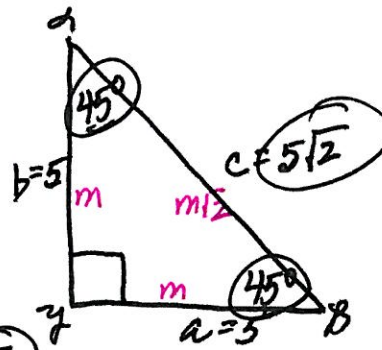
1. $\alpha = 30^\circ$, $b = 20$



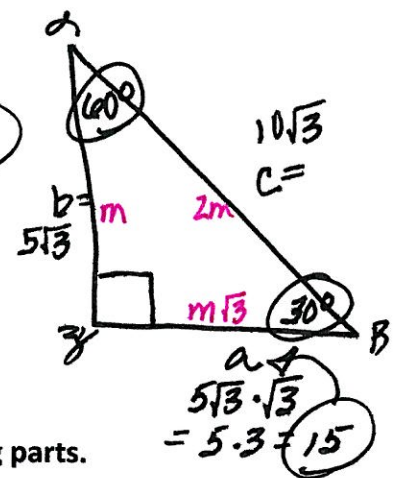
2. $\beta = 45^\circ$, $c = 30$



3. $a = 5$, $b = 5$

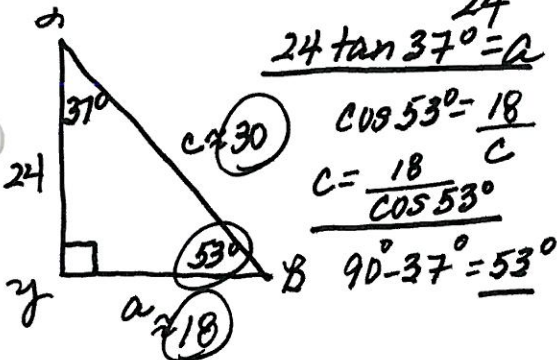


4. $b = 5\sqrt{3}$, $c = 10\sqrt{3}$

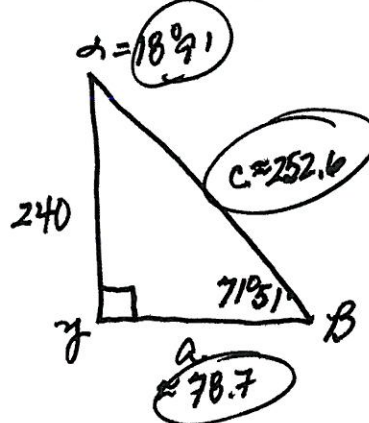


Given the indicated parts of triangle ABC with $\gamma = 90^\circ$, approximate the remaining parts.

5. $\alpha = 37^\circ$, $b = 24$ $\tan 37^\circ = \frac{a}{24}$

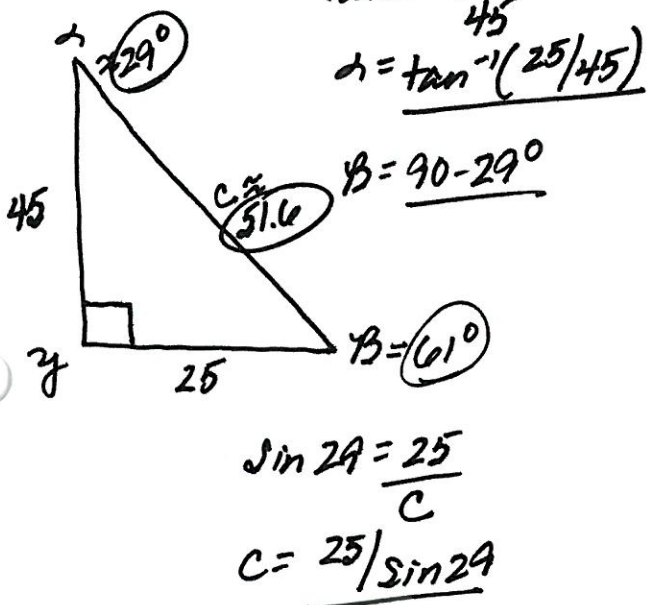


6. $\beta = 71^\circ 51'$, $b = 240.0$

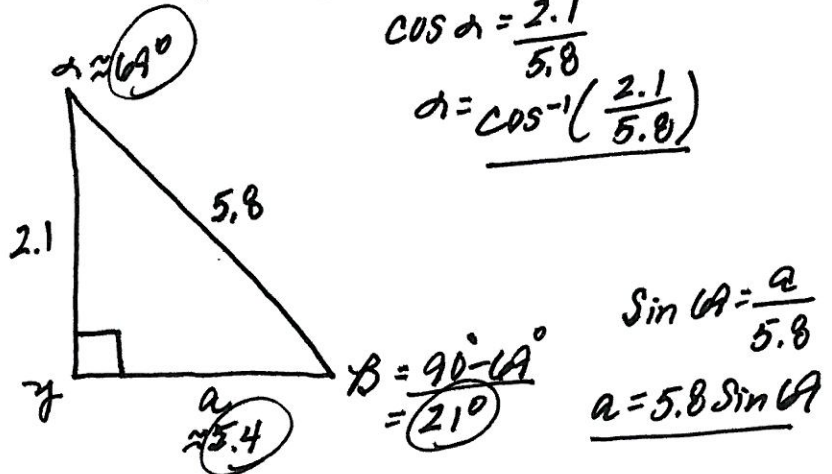


$90^\circ - 71^\circ 51' = \alpha$
 $18^\circ 9' = \alpha$
 $\sin 18^\circ 9' = \frac{a}{252.6}$
 $a = 252.6 (\sin 18^\circ 9')$
 $\sin 71^\circ 51' = \frac{240}{c}$
 $c = \frac{240}{\sin 71^\circ 51'}$

7. $a = 25$, $b = 45$



8. $c = 5.8$, $b = 2.1$



Given the indicated parts of triangle ABC with $\gamma = 90^\circ$, express the third part in terms of the first two.

9. $\alpha, c; b$

$$\cos \alpha = \frac{b}{c}$$

$$b = c \cos \alpha$$

10. $\beta, b; a$

$$\cot \beta = \frac{a}{b}$$

$$a = b \cot \beta$$

11. $\alpha, a; c$

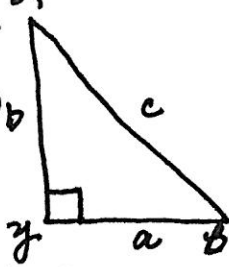
$$\csc \alpha = \frac{c}{a}$$

$$c = a \csc \alpha$$

12. $a, c; b$

$$a^2 + b^2 = c^2$$

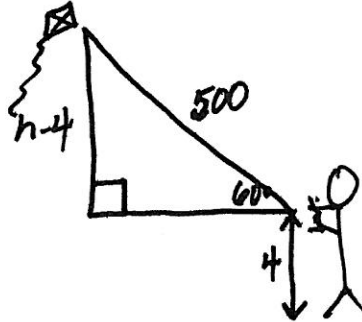
$$b^2 = c^2 - a^2$$

$$b = \sqrt{c^2 - a^2}$$


13. A person flying a kite holds the string 4 feet above ground level. The string of the kite is taut and makes an angle of 60° with the horizontal. Approximate the height of the kite above level ground if 500 feet of string is payed out.

$h = \text{height of kite}$

$$x = h - 4$$



$$\sin 60^\circ = \frac{h-4}{500}$$

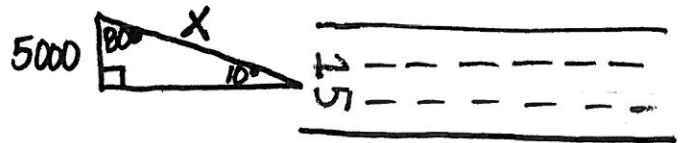
$$h = 437 \text{ ft.}$$

14. A pilot, flying at an altitude of 5000 feet, wishes to approach the numbers on a runway at an angle of 10° . Approximate, to the nearest 100 feet, the distance from the airplane to the numbers at the beginning of the descent.

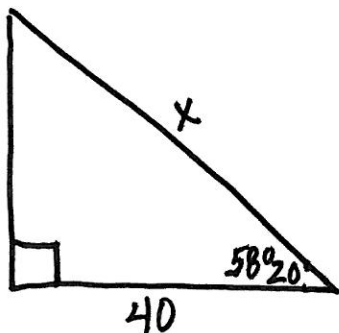
$$\sin 10^\circ = \frac{5000}{x}$$

$$x = 5000 / \sin 10^\circ$$

$$x \approx 28,800 \text{ ft.}$$



15. A guy wire is attached to the top of a radio antenna and to a point on horizontal ground that is 40.0 meters from the base of the antenna. If the wire makes an angle of $58^\circ 20'$ with the ground, approximate the length of the wire.

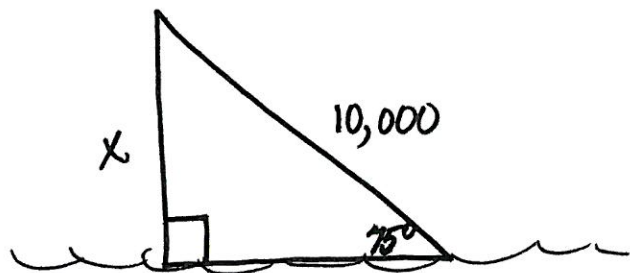


$$\cos 58^\circ 20' = \frac{40}{x}$$

$$x = 40 / \cos 58^\circ 20'$$

$$x \approx 76.2 \text{ m.}$$

16. A rocket is fired at sea level and climbs at a constant angle of 75° through a distance of 10,000 feet. Approximate its altitude to the nearest foot.

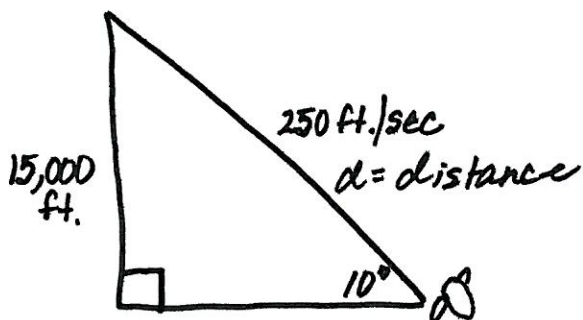


$$\sin 75^\circ = \frac{x}{10,000}$$

$$x = 10,000 (\sin 75^\circ)$$

$$x = 9659 \text{ ft.}$$

17. An airplane takes off at a 10° angle and travels at the rate of 250 ft/sec. Approximately how long does it take the airplane to reach an altitude of 15,000 feet?



$$\sin 10^\circ = \frac{15000}{d}$$

$$d = 15000 / \sin 10^\circ$$

$$d = 86,382 \text{ ft.}$$

$$r \cdot t = d$$

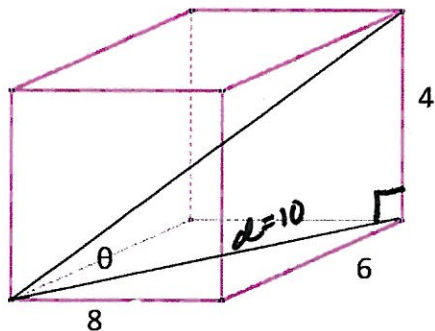
$$(250) t = 86,382$$

$$t = \frac{86382}{250}$$

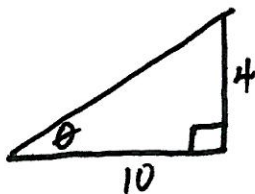
$$t = 345 \text{ sec.}$$

$$\text{or } 345/60 \approx 5.75 \text{ min.}$$

18. A rectangular box has dimensions 8" x 6" x 4". Approximate, to the nearest tenth of a degree, the angle θ formed by a diagonal of the base and the diagonal of the box.



$$\text{diagonal of base} = \sqrt{8^2 + 6^2} = 10$$



$$\tan \theta = \frac{4}{10}$$

$$\theta = \tan^{-1} \left(\frac{4}{10} \right)$$

$$\theta \approx 21.8^\circ$$

