

Find the reference angle θ_R if θ has the given measure.

1. (a) 240°

$240 - 180 = 60^\circ$

(b) 340°

$360 - 340 = 20^\circ$

(c) -202°

$202 - 180 = 22^\circ$

(d) -660°

$360 - 300 = 60^\circ$
 $-660 + 360 = -300$

2. (a) $3\pi/4$

$\pi - \frac{3\pi}{4} = \frac{\pi}{4}$

(b) $4\pi/3$

$\frac{4\pi}{3} - \pi = \frac{\pi}{3}$

(c) $-\pi/6$

$-\frac{\pi}{6}$

(d) $9\pi/4$

$\frac{9\pi}{4} - 2\pi = \frac{\pi}{4}$

3. (a) 3

$\frac{\pi}{2} < 3 < \pi$
 $\pi - 3 \approx .14$

(b) -2

$3.14 - 2 = 1.14$

(c) 5.5

$\frac{3\pi}{2} < 5.5 < 2\pi$
 $6.28 - 5.50 = .78$

(d) 100

$\frac{100}{2\pi} = 15.92$ rev.
 $100 - 15(2\pi) = 5.75$
 $2\pi - 5.75 = .53$

Find the exact value.

4. (a) $\sin(2\pi/3)$

$\frac{\sqrt{3}}{2}$

(b) $\sin(-5\pi/4)$

$\frac{\sqrt{2}}{2}$

5. (a) $\cos 150^\circ$

$-\frac{\sqrt{3}}{2}$

(b) $\cos(-60^\circ)$

$\frac{1}{2}$

6. (a) $\tan(5\pi/6)$

$-\frac{\sqrt{3}}{3}$

(b) $\tan(-\pi/3)$

$-\sqrt{3}$

7. (a) $\cot 120^\circ$

$-\frac{\sqrt{3}}{3}$

(b) $\cot(-150^\circ)$

$\sqrt{3}$

8. (a) $\sec(2\pi/3)$

-2

(b) $\sec(-\pi/6)$

$\frac{2}{\sqrt{3}}$

9. (a) $\csc 240^\circ$

$-\frac{2}{\sqrt{3}}$

(b) $\csc(-330^\circ)$

2

Approximate to three decimal places.

10. (a) $\sin 73^\circ 20'$

.958

(b) $\cos 0.68$

(radian mode)
.778

11. (a) $\tan 21^\circ 10'$

.387

(b) $\cot 1.13$ radian

$1/\tan(1.13)$
.472

12. (a) $\sec 67^\circ 50'$

$1/\cos(67^\circ 50')$
2.650

(b) $\csc 0.32$ radian

$1/\sin .32$
3.179

13. (a) $\csc 43^\circ 40'$

$1/\sin 43^\circ 40' =$
1.448

(b) $\sec 0.26$ radian

$1/\cos .26$
1.035

Approximate the acute angle θ to the nearest (a) 0.01° and (b) $1'$.

14. $\cos \theta = 0.8620$

15. $\tan \theta = 3.7$

16. $\sin \theta = 0.4217$

17. $\sec \theta = 4.246$

$\cos^{-1}(0.8620)$

$\tan^{-1}(3.7)$

$\sin^{-1}(0.4217)$

$\cos \theta = \frac{1}{4.246}$

(a) 30.46°

(a) 74.88°

(a) 24.94°

$\theta = \cos^{-1}\left(\frac{1}{4.246}\right)$

(b) $30^\circ 27'$

(b) $74^\circ 53'$

(b) $24^\circ 57'$

(a) 76.38°

Approximate to four decimal places.

18. (a) $\sin 98^\circ 10'$

(b) $\cos 623.7^\circ$

(c) $\tan 3$ (radian) $\left(\frac{1}{\tan 231^\circ 40'}\right)$

(d) $\cot 231^\circ 40'$

(e) $\sec 1175.1^\circ$

(f) $\csc 0.82$

≈ 0.9899

≈ -0.1097

≈ -0.1425

≈ 0.7907

$\left(\frac{1}{\cos 1175.1}\right)$

(radian) $\left(\frac{1}{\sin .82}\right)$

≈ -11.2493

≈ 1.3677

Approximate, to the nearest 0.1° , all angles θ in the interval $[0^\circ, 360^\circ)$ that satisfy the equation.

19. (a) $\sin \theta = -0.5640$

(b) $\cos \theta = 0.7490$

(c) $\tan \theta = 2.798$

$\sin^{-1}(-0.5640) \approx -34.3^\circ$

$\cos^{-1}(0.7490) = 41.5^\circ$

$\tan^{-1}(2.798) = 70.3^\circ$

$\theta_R = 34.3$ (sin neg in QIII + QIV)

$\theta_R = 41.5^\circ$

$\theta_R = 70.3^\circ$

$180 + 34.3 = 214.3^\circ$

QI: 41.5°

QI: 70.3°

$360 - 34.3 = 325.7^\circ$

QIV: $360 - 41.5 = 318.5^\circ$

QIII: $180 + 70.3 = 250.3^\circ$

(d) $\cot \theta = -0.9601$

(e) $\sec \theta = -1.116$

(f) $\csc \theta = 1.485$

$\tan \theta = \frac{1}{-0.9601}; \theta = \tan^{-1}\left(\frac{1}{-0.9601}\right)$

$\cos \theta = \frac{1}{-1.116}; \theta = \cos^{-1}\left(\frac{1}{-1.116}\right)$

$\sin \theta = \frac{1}{1.485};$

$\theta_R = 46.2^\circ$

$\approx -46.2^\circ$

$\theta = 153.6^\circ$

$\theta = \sin^{-1}\left(\frac{1}{1.485}\right) = 42.3^\circ$

QII: $180 - 46.2 = 133.8^\circ$

$\theta_R = 180 - 153.6 = 26.4^\circ$

$\theta_R = 42.3^\circ$

QIV: $360 - 46.2 = 313.8^\circ$

QII: 153.6°

QI: 42.3°

QIII: $180 + 26.4 = 206.4^\circ$

QII: $180 - 42.3 = 137.7^\circ$

Approximate, to the nearest 0.01 radian, all angles θ in the interval $[0, 2\pi)$ that satisfy the equation.

20. (a) $\sin \theta = 0.4195$

(b) $\cos \theta = -0.1207$

(c) $\tan \theta = -3.2504$

$\sin^{-1}(0.4195) \approx .43; \theta_R = .43$

$\cos^{-1}(-0.1207) \approx 1.69$

$\tan^{-1}(-3.2504) \approx -1.27$

QI: $.43$

$\theta_R = \pi - 1.69 \approx 1.45$

$\theta_R = 1.27$

QII: $\pi - .43 \approx 2.71$

QII: 1.69

QII: $\pi - 1.27 \approx 1.87$

QIII: $\pi + 1.45 \approx 4.59$

QIV: $2\pi - 1.27 \approx 5.01$

(d) $\cot \theta = 2.6815$

$$\tan \theta = \frac{1}{2.6815}$$

$$\theta = \tan^{-1}\left(\frac{1}{2.6815}\right) = \underline{.36}$$

$$\theta_R = .36$$

$$Q.I: \underline{.36}$$

$$Q.III: \pi + .36 \approx \underline{3.50}$$

(e) $\sec \theta = 1.7452$

$$\cos \theta = \frac{1}{1.7452}$$

$$\theta = \cos^{-1}\left(\frac{1}{1.7452}\right) \approx \underline{.96}$$

$$\theta_R = .96$$

$$Q.I: \underline{.96}$$

$$Q.IV: 2\pi - .96 \approx \underline{5.32}$$

(f) $\csc \theta = -4.8521$

$$\sin \theta = \frac{1}{-4.8521}$$

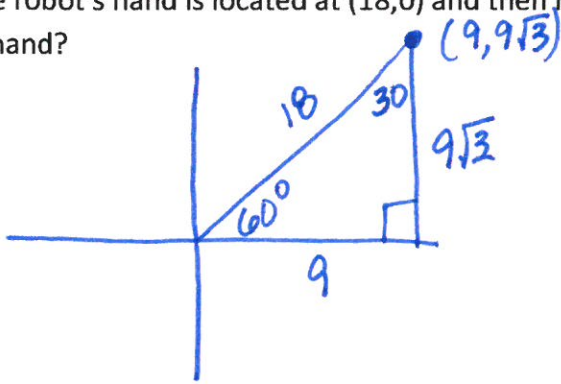
$$\theta = \sin^{-1}\left(\frac{1}{-4.8521}\right) \approx \underline{-.21}$$

$$\theta_R = .21$$

$$Q.III: \pi + .21 \approx \underline{3.35}$$

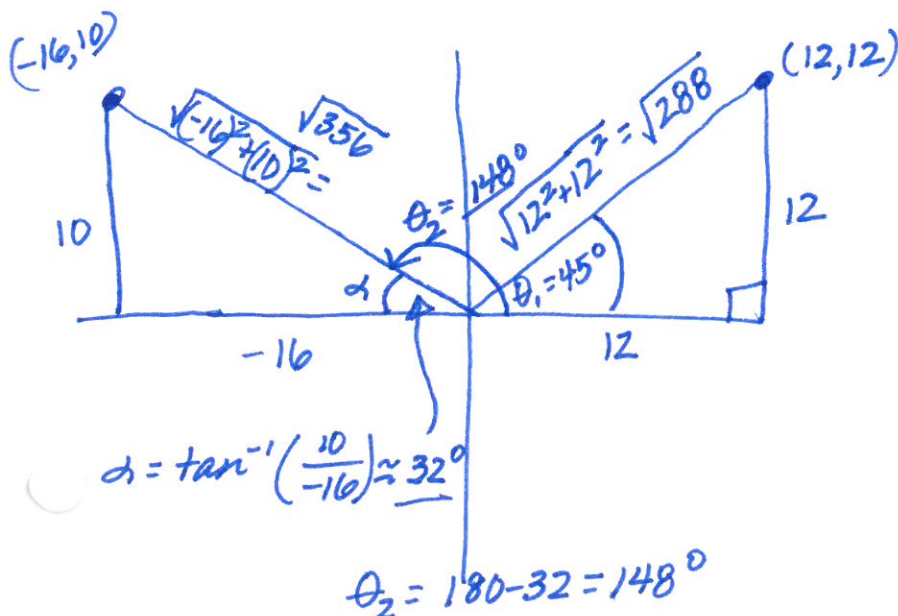
$$Q.IV: 2\pi - .21 \approx \underline{6.07}$$

21. Suppose a robot has a straight arm 18 inches long that can rotate about the origin in a coordinate plane. If the robot's hand is located at (18,0) and then rotates through an angle of 60°, what is the new location of the hand?



$$\underline{(9, 9\sqrt{3})}$$

22. Suppose the robot's arm in #21 can change its length in addition to rotating about the origin. If the hand is initially at (12, 12), approximately how many degrees should the arm be rotated and how much should its length be changed to move the hand to (-16, 10)?



$$\text{rotate } \theta_2 - \theta_1 = 148 - 45 = \underline{103^\circ \text{ CCW}}$$

increase length =

$$\sqrt{356} - \sqrt{288} \approx \underline{1.9 \text{ in}}$$