

*AAT

Chapter 2: 2-4 Complex Numbers (IC/HW)-Day 1

Name: Key
Date: _____ Period: _____

Write the expression in the form $a + bi$, where a and b are real numbers.

1. $(7 - 6i) - (-11 - 3i)$

$$7 - 6i + 11 + 3i$$
$$18 - 3i$$

2. $(-2 + 6i)(8 - i)$

$$-16 + 50i - 6i^2$$
$$-10 + 50i$$

3. $(5 - 2i)^2$

$$(5 - 2i)(5 - 2i)$$
$$25 - 20i + 4i^2$$
$$21 - 20i$$

4. $(3 + 4i)(3 - 4i)$

$$9 - 16i^2$$
$$25$$

5. i^{43}

$$-i$$

6. i^{66}

$$-1$$

7. i^{92}

$$1$$

8. $\frac{(1-7i)(6+2i)}{(6-2i)(6+2i)}$

$$\frac{6 - 40i - 14i^2}{36 - 4i^2} = \frac{20 - 40i}{40}$$
$$= \frac{1}{2} - i$$

9. $\frac{-3-2i}{5+2i} \frac{(5-2i)}{(5-2i)}$

$$\frac{-15 - 4i + 4i^2}{25 - 4i^2} = \frac{-19 - 4i}{29}$$

10. $(2 + 3i)^3$

$$(2 + 3i)(2 + 3i)(2 + 3i)$$
$$(4 + 12i + 9i^2)(2 + 3i)$$
$$(-5 + 12i)(2 + 3i)$$
$$-10 + 9i + 36i^2$$
$$-46 + 9i$$

11. $(-3 + \sqrt{-25})(8 - \sqrt{-36})$

$$(-3 + 5i)(8 - 6i)$$
$$-24 + 58i - 30i^2$$
$$6 + 58i$$

12. $(2 - \sqrt{-4})(3 - \sqrt{-16})$

$$(2 - 2i)(3 - 4i)$$
$$6 - 14i + 8i^2$$
$$-2 - 14i$$

Find the values of x and y , where x and y are real numbers.

13. $4 + (x + 2y)i = x + 2i$

$$\begin{aligned} 4 &= x & x + 2y &= 2 \\ 4 + 2y &= 2 & & \\ 2y &= -2 & & \\ y &= -1 & & \end{aligned}$$

14. $(x - y) + 3i = 7 + yi$

$$\begin{aligned} x - y &= 7 & 3 &= y \\ x - 3 &= 7 & & \\ x &= 10 & & \end{aligned}$$

15. $(2x - y) - 16i = 10 + 4yi$

$$\begin{aligned} 2x - y &= 10 & -16 &= 4y \\ & & \frac{-16}{4} &= \frac{4y}{4} \\ & & -4 &= y \\ 2x - (-4) &= 10 & & \\ 2x + 4 &= 10 & & \\ 2x &= 6 & & \\ x &= 3 & & \end{aligned}$$

Find the solutions of the equation.

16. $x^2 - 6x + 13 = 0$

$$\begin{aligned} x^2 - 6x + 9 &= -13 + 9 \\ \sqrt{(x-3)^2} &= \sqrt{-4} \\ x - 3 &= \pm 2i \\ x &= 3 \pm 2i \end{aligned}$$

17. $x^2 + 4x + 13 = 0$

$$\begin{aligned} x^2 + 4x + 4 &= -13 + 4 \\ \sqrt{(x+2)^2} &= \sqrt{-9} \\ x + 2 &= \pm 3i \\ x &= -2 \pm 3i \end{aligned}$$

18. $x^2 + 3x + 6 = 0$

$$\begin{aligned} x^2 + 3x + \frac{9}{4} &= -6 + \frac{9}{4} \\ \sqrt{\left(x + \frac{3}{2}\right)^2} &= \sqrt{\frac{-15}{4}} \\ x + \frac{3}{2} &= \pm \frac{i\sqrt{15}}{2} \\ x &= -\frac{3}{2} \pm \frac{i\sqrt{15}}{2} \end{aligned}$$