

Determine the values of  $d$  that complete the square for the expression.

1. (a)  $x^2 + 9x + d$

$$\left(\frac{9}{2}\right)^2 = \frac{81}{4}$$

(b)  $x^2 - 8x + d$

$$\left(\frac{8}{2}\right)^2 = 4^2 = 16$$

(c)  $x^2 + dx + 36$

$$\sqrt{36} = 6 \cdot 2 \\ = \pm 12$$

(d)  $x^2 + dx + \frac{49}{4}$

$$\sqrt{\frac{49}{4}} = \frac{7}{2} \cdot 2 \\ = \pm 7$$

2. (a)  $x^2 + 13x + d$

$$\left(\frac{13}{2}\right)^2 = \frac{169}{4}$$

(b)  $x^2 - 6x + d$

$$\left(\frac{6}{2}\right)^2 = 3^2 = 9$$

(c)  $x^2 + dx + 25$

$$\sqrt{25} = 5 \cdot 2 \\ = \pm 10$$

(d)  $x^2 + dx + \frac{81}{4}$

$$\sqrt{\frac{81}{4}} = \frac{9}{2} \cdot 2 \\ = \pm 9$$

Solve by completing the square.

3.  $x^2 + 6x + 7 = 0$

$$x^2 + 6x = -7$$

$$x^2 + 6x + 9 = -7 + 9$$

$$\sqrt{(x+3)^2} = \sqrt{2}$$

$$x+3 = \pm\sqrt{2}$$

$$x = -3 \pm \sqrt{2}$$

4.  $x^2 - 8x + 11 = 0$

$$x^2 - 8x = -11$$

$$x^2 - 8x + 16 = -11 + 16$$

$$\sqrt{(x-4)^2} = \sqrt{5}$$

$$x-4 = \pm\sqrt{5}$$

$$x = 4 \pm \sqrt{5}$$

5.  $4x^2 - 12x - 11 = 0$

$$\frac{4x^2 - 12x}{4} = \frac{11}{4}$$

$$x^2 - 3x + \frac{9}{4} = \frac{11}{4} + \frac{9}{4}$$

$$\sqrt{\left(x - \frac{3}{2}\right)^2} = \sqrt{\frac{20}{4}}$$

$$x - \frac{3}{2} = \pm\sqrt{5}$$

$$x = \frac{3}{2} \pm \sqrt{5}$$

6.  $4x^2 + 20x + 13 = 0$

$$\frac{4x^2 + 20x}{4} = \frac{-13}{4}$$

$$x^2 + 5x + \frac{25}{4} = \frac{-13}{4} + \frac{25}{4}$$

$$\sqrt{\left(x + \frac{5}{2}\right)^2} = \sqrt{\frac{12}{4}}; \quad x + \frac{5}{2} = \pm\sqrt{3}; \quad x = -\frac{5}{2} \pm \sqrt{3}$$

Solve by using the quadratic formula.

7.  $6x^2 - x = 2$

$$6x^2 - x - 2 = 0$$

$$\frac{1 \pm \sqrt{1 - 4(6)(-2)}}{2(6)}$$

$$2(6)$$

$$= \frac{1 \pm \sqrt{49}}{12} = \frac{1 \pm 7}{12}$$

$$x = \frac{8}{12} = \frac{2}{3}; \quad x = \frac{-6}{12} = -\frac{1}{2}$$

8.  $x^2 + 4x + 2 = 0$

$$\frac{-4 \pm \sqrt{16 - 4(1)(2)}}{2(1)}$$

$$\frac{-4 \pm \sqrt{8}}{2} = \frac{-4 \pm 2\sqrt{2}}{2}$$

$$x = -2 \pm \sqrt{2}$$

9.  $2x^2 - 3x - 4 = 0$

$$\frac{3 \pm \sqrt{9 - 4(2)(-4)}}{2(2)}$$

$$2(2)$$

$$\frac{3 \pm \sqrt{41}}{4}$$

$$x = \frac{3 \pm \sqrt{41}}{4}$$

Solve for the specified variable.

10.  $K = \frac{1}{2}mv^2$  for  $v$ .

(Kinetic energy)

$$\frac{2K}{m} = \frac{mv^2}{m}$$

$$\sqrt{\frac{2K}{m}} = \sqrt{v^2}$$
$$\sqrt{\frac{2K}{m}} = v$$

11.  $F = g \frac{mM}{d^2}$  for  $d$ .

(Newton's law of gravitation)

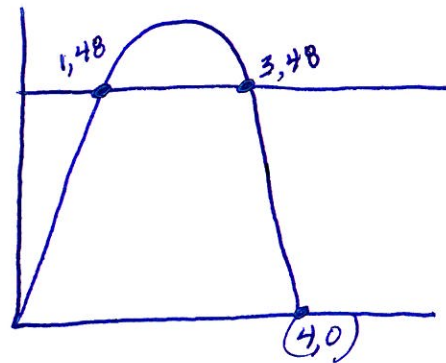
$$d^2 = \frac{gmM}{F}$$

$$d = \sqrt{\frac{gmM}{F}}$$

12. A baseball is thrown straight upward with an initial speed of 64 ft/sec. The number of feet  $s$  above the ground after  $t$  seconds is given by the equation  $s = -16t^2 + 64t$ .

(a) When will the baseball be 48 feet above the ground?

after 1 sec ; after 3 sec.



(b) When will the baseball hit the ground?

after 4 sec.