

Chapter 1: 1-2 Exponents & Radicals (IC/HW)-day 2-3

Name: Key

Date: _____

Period: _____

Express the number in the form a/b , where a and b are integers.

1. $\frac{2^{-3}}{3^{-2}}$

$\frac{3^2}{2^3} = \frac{9}{8}$

2. $(-\frac{3}{2})^4 - 2^{-4}$

$\frac{81}{16} - \frac{1}{16}$
 $= \frac{80}{16} = \frac{5}{1}$

3. $(-0.008)^{2/3}$

$\frac{1}{25}$

4. $\frac{2^0 + 0^2}{2 + 0}$

$\frac{1+0}{2} = \frac{1}{2}$

Simplify.

5. $(4a^{3/2})(2a^{1/2})$

$8a^2$

6. $(8r)^{1/3}(2r^{1/2})$

$2r^{1/3} \cdot 2r^{1/2}$
 $4r^{5/6}$

7. $(8x^{-2/3})x^{1/6}$

$8x^{-3/6}$
 $= \frac{8}{x^{1/2}}$

8. $(\frac{-y^2}{-1})^3$

$\frac{-y^2}{-1} = -y^2$
 $-y^2 = -y^{11/2}$

9. $\frac{(x^6y^3)^{-1}}{(x^4y^2)^{-1}}$

$\frac{x^{-2}y^{-1}}{x^{-2}y^{-1}} = 1$

10. $a^{4/3}a^{-3/2}a^{1/6}$

$a^{0} = 1$

11. $(\frac{c^{-4}}{16d^8})^{3/4}$

$\frac{c^{-3}}{8d^6} = \frac{1}{8c^3d^6}$

12. $(3x^{5/6})(8x^{2/3})$

$24x^{9/6}$
 $= 24x^{3/2}$

Rewrite the expression using rational exponents.

13. $\sqrt[3]{x^5}$

$x^{5/3}$

14. $\sqrt{x^2 + y^2}$

$(x^2 + y^2)^{1/2}$

15. $\sqrt{a + \sqrt{b}}$

$(a + b^{1/2})^{1/2}$

Rewrite the expression using a radical.

16. $4 + x^{3/2}$

$4 + \sqrt{x^3}$
 $4 + x\sqrt{x}$

$\sqrt{x^3}$
 $= \sqrt{x^2 \cdot x}$
 $= x\sqrt{x}$

17. $(4 + x)^{3/2}$

$(4 + x)\sqrt{4 + x}$

18. $(4x)^{3/2}$

$(\sqrt{4x})^3 = 8x\sqrt{x}$

Simplify the expression, and rationalize the denominator when appropriate.

19. $\sqrt[5]{-64}$

$$\sqrt[5]{-32 \cdot 2}$$

$$-2\sqrt[5]{2}$$

20. $\frac{1}{\sqrt[3]{2}} \cdot \frac{\sqrt[3]{4}}{\sqrt[3]{4}} = \frac{\sqrt[3]{4}}{2}$

21. $\sqrt{\frac{1}{7}} \cdot \frac{\sqrt{7}}{\sqrt{7}} = \frac{\sqrt{7}}{7}$

22. $\sqrt{9x^{-4}y^6}$

$$3x^{-2}y^3$$

$$= \frac{3y^3}{x^2}$$

23. $\sqrt[4]{81r^5s^8}$

$$\sqrt[4]{3^4 r^4 s^8}$$

$$3r^1s^2\sqrt[4]{r}$$

24. $\sqrt[3]{\frac{2x^4y^4}{9x}} \cdot \frac{\sqrt[3]{3x^2}}{\sqrt[3]{3x^2}}$

$$= \frac{\sqrt[3]{6x^0y^3 \cdot y}}{3x}$$

$$= \frac{x^2y^3\sqrt[3]{6y}}{3x} = \frac{xy^3\sqrt[3]{6y}}{3}$$

25. $\sqrt[4]{\frac{x^7y^{12}}{125x}} \cdot \frac{5x^3}{5x^3}$

$$\frac{\sqrt[4]{5x^8x^2y^{12}}}{5x} = \frac{x^2y^3\sqrt[4]{5x^2}}{5x}$$

$$= \frac{3x^5}{y^2}$$

$$\rightarrow \frac{xy^3\sqrt[4]{5x^2}}{5}$$

26. $\sqrt[4]{(3x^5y^{-2})^4}$

27. $\sqrt{x^4y^{10}}$

$$x^2y^5$$

28. $\sqrt[4]{x^8(y-1)^{12}}$

$$x^2|y-1|^3$$

29. The length-weight relationship for Pacific halibut can be approximated by the formula $L = 0.46\sqrt[3]{W}$, where W is in kilograms and L is in meters. The largest documented halibut weighed 230 kilograms. Estimate its length.

$$L = 0.46\sqrt[3]{W}$$

$$= 0.46\sqrt[3]{230}$$

$$L = 2.82 \text{ m}$$

30. The length-weight relationship for a whale can be approximated by $W = 0.0016L^{2.43}$, where W is in tons and L is in feet. Estimate the weight of a whale that is 25 feet long.

$$W = 0.0016(25)^{2.43}$$

$$W = 3.99 \text{ tons}$$